## Parachute Inflation and Opening Shock

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**Parachute Seminar** 

3<sup>rd</sup> International Planetary Probe Workshop

## **Outline**

- Maximum parachute structural loads almost always occur during inflation
- Performance predictions frequently require accurate inflation time predictions

# Why Study Parachute Inflation Theory?

- Maximum parachute structural loads almost always occur during inflation
- Performance predictions frequently require accurate inflation time predictions
  - Usually less important than loads

# Is Parachute Inflation Theory a Difficult Topic?

- Fluid Mechanics
  - Unsteady, viscous often compressible flow about a porous body with large shape changes
- Structural Dynamics
  - A tension structure that undergoes large transient deformations

# Is Parachute Inflation Theory a Difficult Topic?

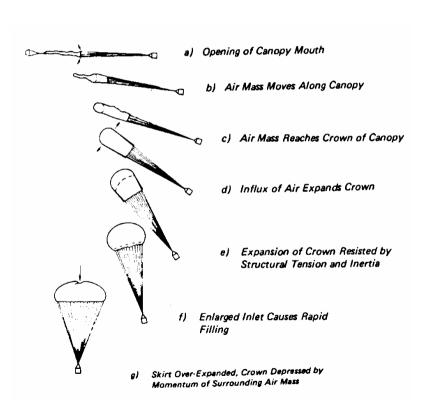
#### Materials

 Nonlinear materials with complex strain, strain rate and hysteresis properties

#### Coupling

All of the above disciplines are strongly coupled

## Parachute Inflation Stages



- Initial inflation until vent pressurized
- Final inflation fro vent pressurization to full open
- Initial inflation can start during deployment
  - Usually desirable

## **Steady Flow Equation**

 Bernoulli equation for steady, inviscid, incompressible flow along a streamline (perfect fluid)

$$\frac{\mathsf{P}}{\rho} + \frac{1}{2} \, \mathsf{V}^2 = \mathsf{C}$$

- P = pressure
- $\rho = density$
- V = velocity
- C = constant

## **Steady Flow Around Sphere**

 Pressure distribution on a sphere in steady, inviscid, incompressible flow (perfect fluid)

$$\frac{\mathsf{P} - \mathsf{P}_{\infty}}{\rho} = \left(\frac{9}{8} \cos^2 \theta - \frac{5}{8}\right) \mathsf{V}^2$$

- $-P_{\infty}$  = pressure far from sphere
- $-\theta$  = angle from stagnation point

## **Steady Flow Drag Force**

Drag force on body in steady flow

$$D = C_d \frac{1}{2} \rho V^2 S$$

- -D = drag
- C<sub>d</sub> = drag coefficient
- -S = area

## **Perfect Fluid Steady Flow**

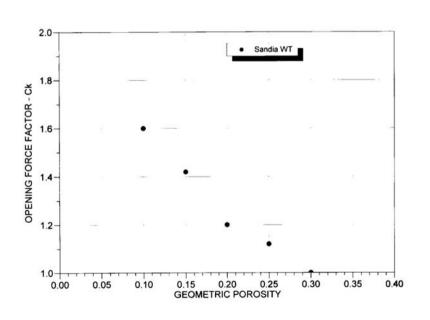
- Simple fluid model gives the correct functional form for drag force
- Shape of pressure distribution and magnitude of drag force are incorrectly predicted
- Real fluid effects due to viscosity and compressibility must be accounted for in pressure and drag coefficients

#### Parachute Opening Shock

- The simplest form of estimating parachute opening shock load is to modify the steady drag equation
  - $F_{\text{max}} = C_k C_d A Q$
  - C<sub>k</sub> is parachute opening shock factor
  - C<sub>d</sub> is parachute drag coefficient
  - A is reference area
  - Q is dynamic pressure

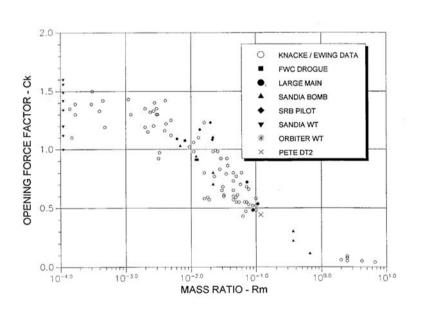
### Parachute Opening Shock Factor

- Infinite mass opening shock factor is primarily a function of canopy porosity
  - Infinite mass implies no deceleration during inflation
  - Maximum load occurs at maximum diameter
- Finite mass opening shock factor is primarily a function of mass ratio (characteristic fluid mass/system mass)
  - Finite mass implies significant deceleration during inflation
  - Acceleration of a large fluid mass (relative to system mass)
     causes system deceleration due to momentum transfer
  - Maximum load occurs early in inflation process

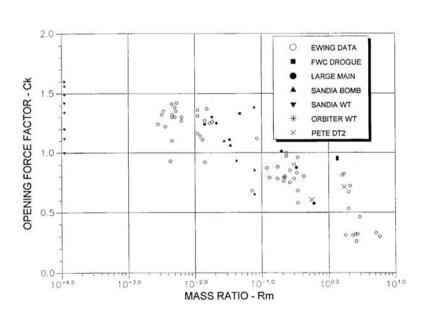


- Wind tunnel data for models with only geometric porosity variations
- Disreefed from nearly closed to full open in steady flow
- High opening shock the result of faster inflation at low porosities

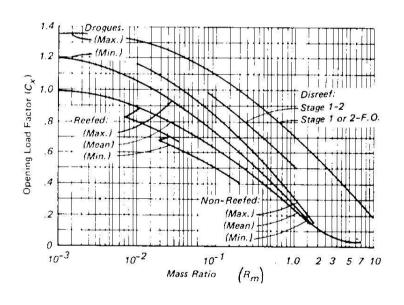
- Finite mass opening shock factor is primarily a function of mass ratio (characteristic fluid mass/system mass)
  - Inverse ratio (system mass/characteristic fluid mass) also sometimes used
- Most common mass ratio used is [ρ(C<sub>d</sub>S)<sup>1.5</sup>/M]
  - Where ρ is atmospheric density
  - C<sub>d</sub>S is parachute drag area
  - M is system mass
- Most extensive correlations
  - Ewing AFFDL-TR-72-3
  - Knacke NWC TP 6575



- For unreefed parachute or inflation to 1<sup>st</sup> reefed stage
- Data from other sources added to Knacke/Ewing data
- Data near Y-axis from infinite mass wind tunnel tests



- For disreef of reefed parachute
- Data from other sources added to Knacke/Ewing data
- Data near Y-axis from infinite mass wind tunnel tests



- Ewing/Bixby/Knacke AFFL-TR-78-151
- Same data set as Knacke/Ewing data
- More specific data correlations from subsets of the data
- Extremes of data scatter shown with mean values

#### Parachute Load Estimates

- Finite mass opening shock factors can be used to provide rapid estimates of parachute opening loads
  - No computer code required
  - Calculator or "back of the envelope" estimate
  - Might need atmosphere table
  - Accurate enough for most parachute design work
  - Quick "sanity check" for computer codes

## **Unsteady Flow Equation**

 Bernoulli equation for unsteady, inviscid, incompressible and irrotational flow along a streamline (perfect fluid)

$$\frac{\mathsf{P}}{\rho} + \frac{1}{2} \mathsf{V}^2 + \frac{\partial \phi}{\partial \mathsf{t}} = \mathsf{C}(\mathsf{t})$$

- $\phi$  = velocity potential (grad  $\phi$  = V)
- -t = time

## **Unsteady Flow Around Sphere**

 Pressure distribution on a sphere in unsteady, inviscid, incompressible and irrotational flow along a streamline (perfect fluid)

$$\frac{\mathsf{P} - \mathsf{P}_{\infty}}{\rho} = \left(\frac{9}{8} \cos^2 \theta - \frac{5}{8}\right) \mathsf{V}^2 + \frac{1}{2} \mathsf{R} \cos \theta \, \frac{\partial \mathsf{V}}{\partial \mathsf{t}}$$

– R = radius of sphere

## **Unsteady Flow Kinetic Energy**

 For the same unsteady flow (unsteady, inviscid, incompressible, irrotational), the fluid kinetic energy can be written

$$T = \frac{1}{2} A_x V_x^2$$

- T = kinetic energy
- $-A_x = a$  fluid mass
- $-V_x$  = velocity of fluid mass (body)

## **Unsteady Flow Force**

 The unsteady fluid force on a body in onedimensional motion is

$$F_{x} = -\frac{d}{dt} \left( \frac{\partial T}{\partial V_{x}} \right) = -A_{x} \frac{dV_{x}}{dt}$$

For a sphere, A<sub>x</sub> can be written

$$A_{x} = C_{ax} \frac{4}{3} \rho \pi R_{p}^{3}$$

 $C_{ax} = 0.5$  (apparent mass coefficient)

 $R_p$  = parachute radius

## **Ballistic Equations of Motion**

 The equations of motion used in most simple trajectory computer codes are the ballistic or zero angle of attack equations

$$(m + A_x)\frac{dV_x}{dt} = m g \sin \gamma - C_d \frac{1}{2}\rho V_x^2 S$$
$$(m + A_x)V_x \frac{d\gamma}{dt} = m g \cos \gamma$$

m = system massg = gravitational accelerationγ = trajectory angle

## **Dimensionless Equations**

The ballistic equations can be written in dimensionless form

$$\frac{dV_{x^*}}{dt^*} = \frac{\sin \gamma}{F_r \left(1 + \frac{C_{ax}}{K_t}\right)} - \frac{\frac{3}{8} C_d V_x^2}{\left(K_t + C_{ax}\right)}$$

$$\frac{d\gamma}{dt^*} = \frac{K_t \cos \gamma}{F_r V_{x^*} (K_t + C_{ax})}$$

## <u>Dimensionless Variables and</u> <u>Parameters</u>

Dimensionless Variables

$$V_{x^*} = \frac{V_x}{V_0}$$
;  $t^* = \frac{t V_0}{R_p}$ 

Dimensionless Parameters

$$F_{r} = \frac{V_{0}^{2}}{gR_{p}}$$
;  $K_{t} = \frac{m}{\frac{4}{3}\rho\pi R_{p}^{3}}$ 

 $V_0$  = initial velocity

## Unsteady Flow Around Expanding Decelerating Sphere

 Pressure distribution on an expanding, decelerating sphere in inviscid, incompressible and irrotational flow

$$\frac{P - P_{\infty}}{\rho} = \left(\frac{9}{8}\cos^2\theta - \frac{5}{8}\right)V_x^2 + \frac{1}{2}R\cos\theta \frac{dV_x}{dt}$$
$$+ \frac{3}{2}V_r^2 + R\frac{dV_r}{dt} + \frac{3}{2}\cos\theta V_x V_r$$
$$V_r = \frac{dR}{dt}$$

### <u>Unsteady Forces on Inflating,</u> <u>Decelerating Parachute</u>

Axial force along flight path

$$F_{xu} = -\left(A_x \frac{dV_x}{dt} + V_x \frac{dA_x}{dt}\right)$$

Radial force

$$F_{ru} = -\left(A_r \frac{dV_r}{dt} + V_r \frac{dA_r}{dt}\right)$$

No axial/radial coupling

### <u>Dimensional Analysis and Unsteady</u> <u>Flow Conclusions</u>

 Dimensional analysis identifies dimensionless parameters that influence opening shock and inflation time

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- Mass ratio K_t = m / [(4/3) \rho \pi R_p^3]
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- Froude number  $F_r = V_0^2 / (g R_p)$
- Simplified perfect fluid analysis provides insight into functional form of forces and pressure distributions

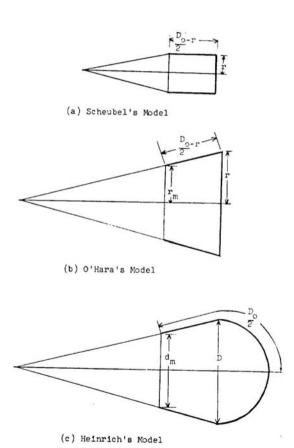
#### **Drag Area vs Time Inflation Models**

- Simplest models specified drag area vs time as input to a point mass trajectory code
  - Inflation times often artificially adjusted to match loads
  - Inflation times sometimes scaled using dimensionless time
- Use of drag area as an independent variable in trajectory codes explains use of drag area directly to calculate mass ratio
- Combined use of point mass computer code and the mass ratio C<sub>k</sub> correlations improved use of this method

#### **Continuity Equation Inflation Models**

- More sophisticated models solved a conservation of mass equation for the parachute internal volume
  - Mass flow in determines rate of change of internal volume
  - Similar shapes used to get diameter and parachute drag
- Calculated shapes combined with point mass trajectory code
  - Apparent mass often used in equations of motion
- Extensive work by U. of Minnesota Dr. Heinrich

## Similar Shapes Used in Continuity Equation Inflation Models



- Early shapes were simple because calculations were manual
- More realistic shapes allowed using computers
- Inflow and outflow assumptions required

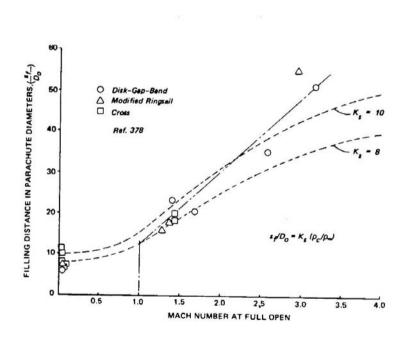
### **Constant Distance Theory Models**

- Another family of inflation models was based on the observation that "a parachute always inflates in a fixed distance traveled"
- This assumption is equivalent to the conservation of mass assumption
  - A column of air ahead of the parachute eventually occupies the internal volume

#### **Constant Distance Theory Models**

- Both the conservation of mass and constant distance theory models assume dynamic similarity in the inflation process
  - Parachute mass ratio doesn't change much
- Instead of similar shapes, radial velocity can be directly specified to be a function of axial velocity
- A compressibility correction to constant distance theory was proposed

#### **Proposed Compressibility Correction**

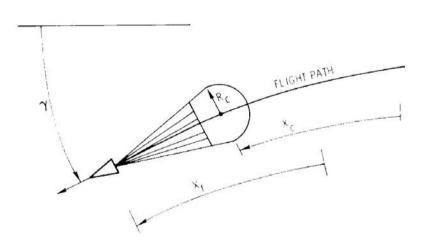


- Compressibility correction assumed normal shock ahead of canopy for density correction
- Wind tunnel photo and drag data show this is incorrect
  - Actual density change is small fraction of normal shock correction

## **Simple Dynamic Inflation Model**

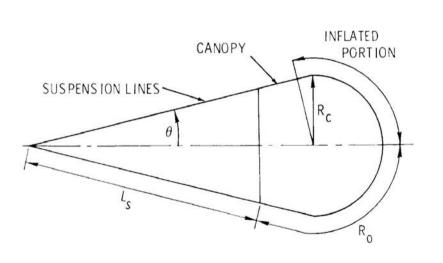
- Model based on conservation of momentum
  - Parachute inflation is a dynamics problem, not a quasi-static problem
  - Single radial degree of freedom
  - Rigid coupling parachute and payload
  - Unreefed parachutes only
  - Steady and unsteady aerodynamic effects

## **Trajectory for Model**



- Ballistic (zero angle of attack) trajectory
- Velocity at payload and parachute different because parachute moves toward payload during inflation

#### Parachute Geometry for Model



#### Similar shapes

- Hemispherical inflated part
- Conical uninflated part
- Rigid coupling between parachute and payload

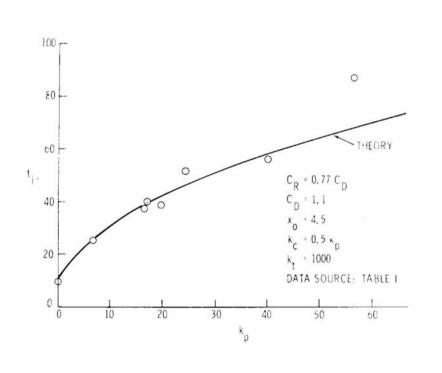
### **Simple Dynamic Inflation Model**

- Single canopy mass element located at maximum diameter point
- Steady radial force coefficient data based on inflated geometry
- Radial force to drag force ratio required to produce canopy shape was obtained from photographic data

### **Simple Dynamic Inflation Model**

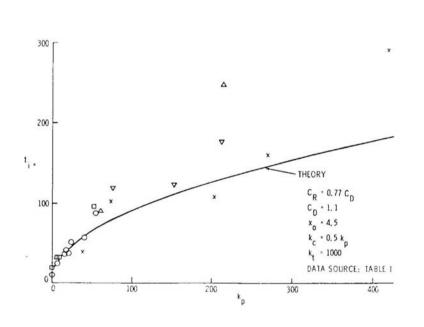
- Equations were put in non-dimensional form
  - A second mass ratio, the parachute mass ratio, was revealed
- Predictions of the model were compared with test data from the PEPP tests
- Predicted inflation time variations over the wide altitude range of tests agreed very well with PEPP data

### Non-dimentional Inflation Times for DGB Parachutes



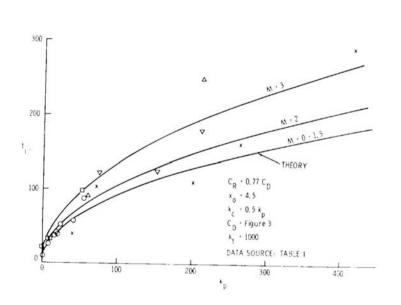
- Dimensionless inflation times correlated well with parachute mass ratio over wide altitude range
  - No compressibility correction

## Non-dimentional Inflation Times for all PEPP Parachutes



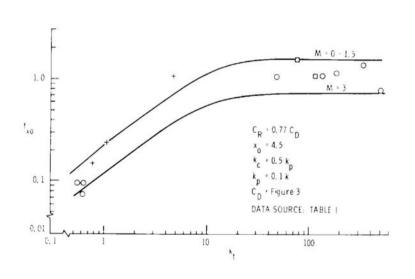
- Dimensionless inflation times correlated well with lower bound of data
- No compressibility correction

## Non-dimentional Inflation Times for all PEPP Parachutes



 Dimensionless inflation times with compressibility corrections based on density estimate required for drag coefficient vs Mach number variation

### Opening Shock Factor for all PEPP Parachutes



- Drag coefficient vs Mach number from wind tunnel data
- Predictions span range of data scatter

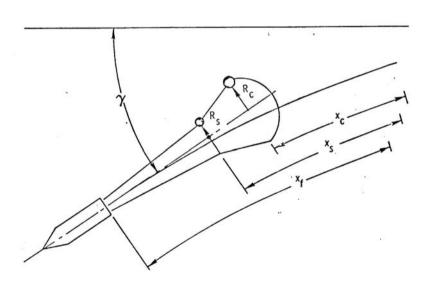
# Conclusions from Simple Dynamic Inflation Model Study

- Parachute mass ratio should be considered an important scaling factor for use of parachutes in low density environment
- Compressibility correction appears to be much less than proposed for constant distance theory models

#### **More General Dynamic Inflation Model**

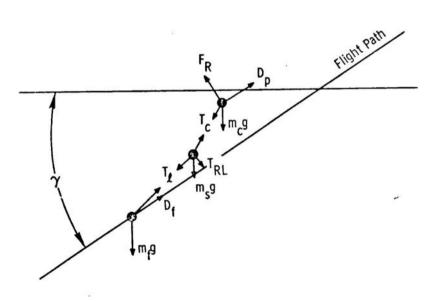
- Two radial degrees of freedom
- Elastic elements couple parachute masses and payload
- Can be used to model reefed parachutes
- Parametric aerodynamic data for different porosities measured to provide design data base

### **Trajectory for Model**



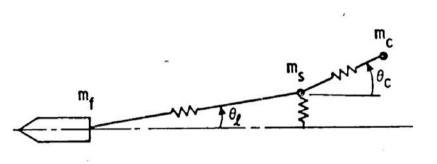
- Ballistic (zero angle of attack) trajectory
- Velocity at payload and parachute different because parachute moves toward payload during inflation

### **Forces on Mass Elements**



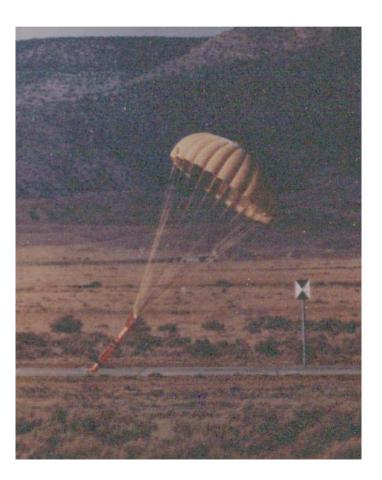
- Two parachute mass elements
  - Maximum diameter
  - Skirt
- Radial force applied at maximum diameter element

# Elastic Constraints on Mass Elements



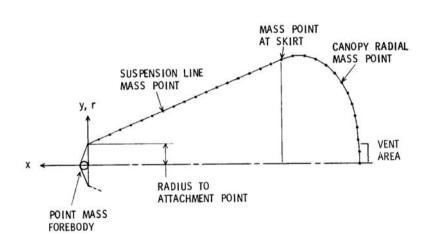
- Allows different elastic properties for suspension lines and radials
- Realistic modeling of reefing line constraint and cutting of reefing line

## **Use of Dynamic Inflation Model**



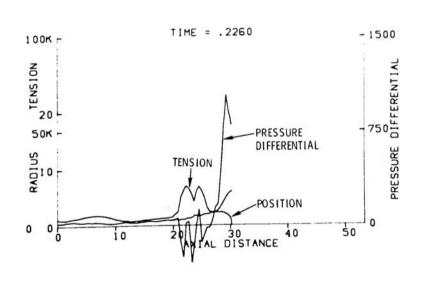
- Used to design many parachutes at Sandia
- Reefing easy to include
- Also used to study wake overtake which occurs during rapid deceleration

# Multi-Element Dynamic Inflation Model



- Many mass elements used to model parachute
- Used to study parachute deployment and inflation in greater detail

# Multi-Element Dynamic Inflation Model



 Used to study variations of tension, radius, pressure and other variables along length of parachute

